

TABLA DE INTEGRALES DEFINIDAS

1	$\int_0^{\infty} x^{n-1} e^{-x} dx = \Gamma(n)$	9	$\int_0^{\infty} x^{m-1} (1-x)^{n-1} dx = \frac{\Gamma(n)\Gamma(m)}{\Gamma(m+n)}$
2	$\int_0^{\infty} \sin(x^2) dx = \int_0^{\infty} \cos(x^2) dx = \frac{1}{2} \sqrt{\frac{f}{2}}$	10	$\int_0^{\infty} \frac{x^{m-1}}{1+x^n} dx = \frac{f/n}{\sin(\pi f/n)} \quad n > m > 0$
3	$\int_0^{\infty} \frac{\sin(x) \cos(nx)}{x} dx = \begin{cases} f/2 & n^2 < 1 \\ f/4 & n^2 = 1 \\ 0 & n^2 > 1 \end{cases}$	11	$\int_0^{\infty} x^n e^{-ax} dx = \frac{n!}{a^{n+1}} \quad n \geq 1, a > 0$
4	$\int_0^{\infty} \frac{\sin^2(x)}{x^2} dx = \frac{f}{2}$	12	$\int_0^{\infty} e^{-a^2 x^2} dx = \frac{1}{2a} \sqrt{f} \quad a > 0$
5	$\int_0^{\infty} \frac{\cos(nx)}{1+x^2} dx = \frac{f}{2} e^{- n }$	13	$\int_0^{\infty} x^2 e^{-x^2} dx = \frac{1}{4} \sqrt{f}$
6	$\int_0^{\infty} \sin c(x) dx = \int_0^{\infty} \sin c^2(x) dx = \frac{1}{2}$	14	$\int_0^{\infty} e^{-ax} \cos(x) dx = \frac{a}{1+a} \quad a > 0$
7	$\int_0^{\infty} \frac{\sin(x)}{x} dx = \int_0^{\infty} \frac{\tan(x)}{x} dx = \frac{f}{2}$	15	$\int_0^{\infty} e^{-ax} \sin(x) dx = \frac{1}{1+a^2} \quad a > 0$
8	$\int_0^{\infty} \sqrt{x} e^{-ax} dx = \frac{1}{2a} \sqrt{\frac{f}{a}}$	16	$\int_0^{\infty} e^{-a^2 x^2} \cos(bx) dx = \frac{1}{2a} e^{-\left(\frac{b}{2a}\right)^2}$

TABLA DE INTEGRALES INDEFINIDAS IMPORTANTES

1	$\int x e^{ax} dx = \frac{1}{a^2} e^{ax} (ax - 1) + c$
2	$\int x^2 e^{ax} dx = \frac{1}{a^3} e^{ax} [\operatorname{Arcsen}(ax) - 2ax + 2] + c$
3	$\int e^{ax} \sin(bx) dx = \frac{1}{a^2+b^2} e^{ax} [a \sin(bx) - b \cos(bx)] + c$
4	$\int e^{ax} \cos(bx) dx = \frac{1}{a^2+b^2} e^{ax} [a \cos(bx) + b \sin(bx)] + c$
5	$\int x \sin(ax) dx = \frac{1}{a^2} [\sin(ax) - ax \cos(ax)] + c$
6	$\int x \cos(ax) dx = \frac{1}{a^2} [\cos(ax) + ax \sin(ax)] + c$
7	$\int x^2 \sin(ax) dx = \frac{2x}{a^3} \sin(ax) + \frac{2}{a^3} \cos(ax) - \frac{x^2}{a} \cos(ax) + c$
8	$\int x^2 \cos(ax) dx = \frac{2x}{a^2} \cos(ax) - \frac{2}{a^3} \sin(ax) \frac{x^2}{a} \sin(ax) + c$
9	$\int \cos(ax) \cos(bx) dx = \frac{1}{2} \left[\frac{\sin((a-b)x)}{a-b} + \frac{\sin((a+b)x)}{a+b} \right] + c \quad a^2 \neq b^2$

10	$\int \sin(ax)\cos(bx)dx = -\frac{1}{2} \left[\frac{\cos[(a-b)x]}{a-b} + \frac{\cos[(a+b)x]}{a+b} \right] + c \quad a^2 \neq b^2$
11	$\int \sin(ax)\sin(bx)dx = -\frac{1}{2} \left[\frac{\sin[(a-b)x]}{a-b} - \frac{\sin[(a+b)x]}{a+b} \right] + c \quad a^2 \neq b^2$
12	$\int x \sin^2(ax)dx = \frac{x^2}{4} - \frac{x \sin(2ax)}{4a} - \frac{\cos(2ax)}{8a^2} + c$
13	$\int x \cos^2(ax)dx = \frac{x^2}{4} + \frac{\sin(2ax)}{4a} - \frac{\cos(2ax)}{8a^2} + c$
14	$\int \sin^n(ax)\cos(ax)dx = -\frac{1}{a(n+1)} \sin^{n+1}(ax) + c \quad n \neq -1$
15	$\int \cos^n(ax)\sin(ax)dx = \frac{1}{a(n+1)} \cos^{n+1}(ax) + c \quad n \neq -1$

TABLA DE IDENTIDADES TRIGONOMÉTRICAS

1	$\sin(w_1 t \pm w_2 t) = \sin(w_1 t)\cos(w_2 t) \pm \cos(w_1 t)\sin(w_2 t)$	15	$\sin^2(wt) + \cos^2(wt) = 1$
2	$\cos(w_1 t \pm w_2 t) = \cos(w_1 t)\cos(w_2 t) \mp \sin(w_1 t)\sin(w_2 t)$	16	$\sin^2(wt) = \frac{1 - \cos(2wt)}{2}$
3	$\sin(w_1 t) + \sin(w_2 t) = 2 \sin\left(\frac{w_1 t + w_2 t}{2}\right) \cos\left(\frac{w_1 t - w_2 t}{2}\right)$	17	$\cos^2(wt) = \frac{1 + \cos(2wt)}{2}$
4	$\sin(w_1 t) - \sin(w_2 t) = 2 \sin\left(\frac{w_1 t - w_2 t}{2}\right) \cos\left(\frac{w_1 t + w_2 t}{2}\right)$	18	$1 + \operatorname{ctg}^2(wt) = \operatorname{csc}^2(x)wt$
5	$\cos(w_1 t) + \cos(w_2 t) = 2 \cos\left(\frac{w_1 t + w_2 t}{2}\right) \cos\left(\frac{w_1 t - w_2 t}{2}\right)$	19	$1 + \operatorname{tg}^2(wt) = \operatorname{sec}^2(wt)$
6	$\cos(w_1 t) - \cos(w_2 t) = -2 \sin\left(\frac{w_1 t + w_2 t}{2}\right) \sin\left(\frac{w_1 t - w_2 t}{2}\right)$	20	$\sin(2wt) = 2 \sin(wt) \cos(wt)$
7	$\operatorname{tg}(w_1 t) \pm \operatorname{tg}(w_2 t) = \frac{\sin(w_1 t \pm w_2 t)}{\cos(w_1 t) \cos(w_2 t)}$	21	$\cos(2wt) = \cos^2(wt) - \sin^2(wt)$
8	$\cos(w_1 t)\cos(w_2 t) = \frac{1}{2} [\cos(w_1 t + w_2 t) + \cos(w_1 t - w_2 t)]$	22	$\sin(3wt) = 3 \sin(wt) - 4 \sin^3(wt)$
9	$\sin(w_1 t)\cos(w_2 t) = \frac{1}{2} [\sin(w_1 t + w_2 t) + \sin(w_1 t - w_2 t)]$	23	$\cos(3wt) = 4 \cos^3(wt) - 3 \cos(wt)$
10	$\sin(w_1 t)\sin(w_2 t) = \frac{1}{2} [\cos(w_1 t - w_2 t) - \cos(w_1 t + w_2 t)]$	24	$\sin\left(\frac{wt}{2}\right) = \pm \sqrt{\frac{1 - \cos(wt)}{2}}$
11	$\sin(4wt) = 8 \cos^3(wt) \sin(wt) - 4 \cos(wt) \sin(wt)$	25	$\cos\left(\frac{wt}{2}\right) = \pm \sqrt{\frac{1 + \cos(wt)}{2}}$
12	$\cos(4wt) = 8 \cos^4(wt) - 8 \cos^2(wt) + 1$	26	$\operatorname{tg}\left(\frac{wt}{2}\right) = \frac{\sin(wt)}{1 + \cos(wt)}$
13	$\cos(wt) = \cos\left(\frac{f}{2} - wt\right) = -\cos(f - wt)$		
14	$\sin(wt) = \cos\left(\frac{f}{2} - wt\right) = \sin(f - wt)$		

TABLA DE IDENTIDADES COMPLEJAS

$z = x + jy$	$z = z e^{j\theta} \quad \theta = \arg(z)$
$ z = \sqrt{x^2 + y^2} \quad \wedge \quad \theta = \arg(z) = \arctg\left(\frac{y}{x}\right)$	$ e^{j\theta} = 1$
$\arg(z_1 \cdot z_2) = \arg(z_1) + \arg(z_2)$	$e^{j\theta_1} e^{j\theta_2} = e^{j(\theta_1 + \theta_2)}$
$\arg\left(\frac{z_1}{z_2}\right) = \arg(z_1) - \arg(z_2)$	$e^{-j\theta} = \frac{1}{e^{j\theta}}$
$e^z = e^{x+jy}$	$\frac{e^{j\theta_1}}{e^{j\theta_2}} = e^{j(\theta_1 - \theta_2)}$
$e^z \neq 0 \quad \forall z \in \mathbb{C}$	$(e^{j\theta})^k = e^{jk\theta}$
$ e^z = e^{x+jy} = e^x e^{jy} ^1 = e^x \quad y = \arg(e^z)$	$e^{\pm j\omega t} = \cos(\omega t) \pm j \sin(\omega t)$
$z_1 \cdot z_2 = z_1 \cdot z_2 e^{j[\arg(z_1) + \arg(z_2)]}$	$\cos(\omega t) = \sin\left(\omega t + \frac{\pi}{2}\right) = \frac{e^{j\omega t} + e^{-j\omega t}}{2}$
$\frac{z_1}{z_2} = \frac{ z_1 }{ z_2 } e^{j[\arg(z_1) - \arg(z_2)]}$	$\sin(\omega t) = \cos\left(\omega t - \frac{\pi}{2}\right) = \frac{e^{j\omega t} - e^{-j\omega t}}{2j}$

TABLA DE RESULTADOS GENERALES

FUNCIÓN	n	n PAR	n IMPAR	$\frac{n}{2}$ PAR	$\frac{n}{2}$ IMPAR
$\sin(nf)$	0	0	0	0	0
$\cos(nf)$	$(-1)^n$	+1	-1	+1	+1
$\sin\left(n\frac{f}{2}\right)$		0	$(-1)^{\frac{n-1}{2}}$	0	0
$\cos\left(n\frac{f}{2}\right)$		$(-1)^{\frac{n}{2}}$	0		
$\sin\left[(n \pm 1)\frac{f}{2}\right]$		$\pm(-1)^{\frac{n}{2}}$	0		
$\cos\left[(n \pm 1)\frac{f}{2}\right]$		0	$\pm(-1)^{\frac{n+1}{2}}$		
$\sin\left[(2n \pm 1)\frac{f}{2}\right]$	$\pm(-1)^n$				
$\cos\left[(2n \pm 1)\frac{f}{2}\right]$	0				
$e^{\pm j2fn}$	1	1	1		
$e^{\pm jfn}$	$(-1)^n$	+1	-1		
$e^{jf\frac{n}{2}}$		$(-1)^{\frac{n}{2}}$	$j(-1)^{\frac{n-1}{2}}$		
$e^{\pm j(2n-1)f}$	-1				

PROPIEDADES DE LA FUNCIÓN IMPULSO

$\int_{-\infty}^{\infty} u(t) dt = 1$	$u(t-\frac{a}{2}) = \frac{d}{dt} [u(t-\frac{a}{2})]$
$\int_{-\infty}^{\infty} x(t)u(t-\frac{a}{2}) dt = x(\frac{a}{2})$	$u(a \cdot t) = \frac{1}{ a } u(t)$
$\int_{-\infty}^{\infty} u^{(n)}(t) dt = 0 \quad n \leq 0 \quad n \in \mathbb{Z}$	$[f(t) \cdot u(t)]' = f(t)u'(t) + f'(t)u(t)$
$\int_{-\infty}^{\infty} x(t)u(at) dt = \frac{1}{ a }x(0)$	$\int_{-\infty}^{\infty} \{ (t)u^{(n)}(t-\frac{a}{2}) dt = (-1)^n \{^{(n)}(\frac{a}{2})$
$\int_a^b \{ (t)u^{(n)}(t \pm \frac{a}{2}) dt = \begin{cases} 0 & b < \frac{a}{2} < a \\ \{(\frac{a}{2}) & a \leq \frac{a}{2} \leq b \end{cases}$	$x(t)u^{(n)}(t \pm \frac{a}{2}) = \sum_{k=0}^n \binom{n}{k} (-1)^{n-k} x^{(n-k)}(-\frac{a}{2})u^{(k)}(t \pm \frac{a}{2})$
$u(-t) = u(t)$	$t \cdot u'(t) = -u(t)$
$t \cdot u(t) = 0$	

PROPIEDADES DE LA SERIE DE FOURIER DE TIEMPO CONTINUO

$f(t)$ y $g(t)$ señales periódicas de periodo T y frecuencia fundamental $w_0 = \frac{2\pi}{T}$, con r y s constantes

f_n y g_n coeficientes de la serie compleja de Fourier de $f(t)$ y $g(t)$ respectivamente

d_n Coeficiente de la serie de Fourier resultado de aplicar la propiedad

PROPIEDAD	SEÑAL	COEFICIENTE $d_n =$
Linealidad	$r f(t) + s g(t)$	$r f_n + s g_n$
Desplazamiento en el tiempo	$f(t \mp t_0)$	$e^{\mp jnw_0 t_0} f_n$
Desplazamiento en frecuencia	$e^{jMw_0 t} = e^{jM \frac{2\pi}{T} t} f(t)$	f_{n-M}
Conjugación	$\bar{f}(t)$	\bar{f}_{-n}
Inversión en el tiempo	$f(-t)$	f_{-n}
Escalamiento en el tiempo	$f(rt) \quad r > 0 \quad T = \frac{T}{a}$	f_n
Cambio de periodo	$f_T(t) \rightarrow f_{nT}(t)$	$\begin{cases} f_{\frac{n}{m}} & \frac{n}{m} \text{ es un entero} \\ 0 & \text{otro caso} \end{cases} \quad \text{con periodo } mT$
Convolución periódica	$\int_T f(t) g(t-\frac{a}{2}) dt$	$T f_n g_n$
	$\frac{1}{T} \int_T s(t) e^{-jn w_0 t} dt$	$f_n g_n$
Multiplicación	$f(t)g(t)$	$\sum_{m=-\infty}^{\infty} f_m g_{n-m} = f_n \otimes g_n$
Diferenciación	$f'(t) = \frac{d f(t)}{dt}$	$(jnw_0) f_n \quad n \neq 0$
Integración	$\int_{-\infty}^t f(\frac{t}{2}) d\frac{t}{2} \Leftrightarrow f_0 = 0$	$\begin{cases} \frac{1}{jnw_0} f_n & n \neq 0 \\ - \sum_{n=-\infty, n \neq 0}^{\infty} \frac{(-1)^n}{jnw_0} f_n & n = 0 \end{cases}$

Simetría conjugada para señales reales	$f(t) \in \text{IR}$	$\begin{cases} f_n = \bar{f}_{-n} \\ \text{Re}(f_n) = \text{Re}(f_{-n}) \\ \text{Im}(f_n) = -\text{Im}(f_{-n}) \end{cases} \quad \begin{cases} f_n = f_{-n} \\ w_n = -w_{-n} \end{cases}$	
Señal real y par	$f(t) \in \text{IR}$ y par	$f_n \in \text{IR}$ y par	
Señal real e impar	$f(t) \in \text{IR}$ e impar	$f_n \in \text{Im}$ e impar	
Descomposición par e impar de señales reales	$f_P(t) \in \text{IR}$ $f_I(t) \in \text{IR}$	$\text{Re}(f_n)$ $-j \text{Im}(f_n)$	
Teorema de Parseval		$\frac{1}{T} \int_{-T/2}^{T/2} [f(t)]^2 dt = \frac{1}{4} a_0^2 + \frac{1}{2} \sum_{n=1}^{\infty} (a_n^2 + b_n^2)$ para serie trigonométrica $\frac{1}{T} \int_T f(t) ^2 dt = \sum_{n=-\infty}^{\infty} f_n ^2 = f_0 + \frac{1}{2} \sum_{n=1}^{\infty} f_n ^2$ para la serie exponencial	

TABLA DE SERIES DE FOURIER

SEÑAL	SERIE TRIGONOMÉTRICA
$f(t) = t \quad -f < t < f$	$f(t) = 2 \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n} \sin(nt)$
$f(t) = t \quad -f < t < f$	$f(t) = \frac{f}{2} - \frac{4}{f} \sum_{n=1}^{\infty} \frac{\cos[(2n-1)t]}{(2n-1)^2}$
$f(t) = f - t \quad 0 < t < 2f$	$f(t) = 2 \sum_{n=1}^{\infty} \frac{\sin(nt)}{n}$
$f(t) = \begin{cases} 0 & -f < t < 0 \\ t & 0 < t < f \end{cases}$	$f(t) = \frac{f}{4} - \frac{2}{f} \sum_{n=1}^{\infty} \frac{\cos[(2n-1)t]}{(2n-1)^2} + \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n} \sin(nt)$
$f(t) = \begin{cases} -1 & -f < t < 0 \\ 1 & 0 < t < f \end{cases}$	$f(t) = \frac{4}{f} \sum_{n=1}^{\infty} \frac{\sin[(2n-1)t]}{2n-1}$
$f(t) = \begin{cases} 0 & -f < t < 0 \\ 1 & 0 < t < f \end{cases}$	$f(t) = \frac{1}{2} + \frac{2}{f} \sum_{n=1}^{\infty} \frac{\sin[(2n-1)t]}{2n-1}$
$f(t) = \sin(t) \quad -f < t < f$	$f(t) = \frac{2}{f} - \frac{4}{f} \sum_{n=1}^{\infty} \frac{\cos(2nt)}{4n^2 - 1}$
$f(t) = \cos(t) \quad -f < t < f$	$f(t) = \frac{2}{f} - \frac{4}{f} \sum_{n=1}^{\infty} \frac{(-1)^n \cos(2nt)}{4n^2 - 1}$
$f(t) = \begin{cases} 0 & -f < t < 0 \\ \sin(t) & 0 < t < f \end{cases}$	$f(t) = \frac{1}{f} - \frac{2}{f} \sum_{n=1}^{\infty} \frac{\cos(2nt)}{4n^2 - 1} - \frac{1}{2} \sin(t)$
ONDA PERIÓDICA	COEFICIENTE DE FOURIER
$f(t) = \sum_{m=-\infty}^{\infty} A \Pi\left(\frac{t-mT}{\frac{\pi}{f}}\right)$ † anchura del pulso	$f_n = A \frac{\sin\left(nw_0 \frac{\pi}{2}\right)}{f_n} = \frac{A\pi}{T} \sin c\left(\frac{nw_0\pi}{2f}\right)$

$f(t) = \sum_{m=-\infty}^{\infty} A\Pi\left(\frac{t-mT}{\frac{\Delta}{2}}\right) \cos(w_p t)$	$f_n = \frac{A\Delta}{2T} \left\{ \sin c\left[\left(\frac{nw_0 - w_p}{2f}\right)\frac{\Delta}{2}\right] + \sin c\left[\left(\frac{nw_0 + w_p}{2f}\right)\frac{\Delta}{2}\right] \right\}$
$f(t) = \sum_{m=-\infty}^{\infty} A\Delta\left(\frac{t-mT}{2\Delta}\right)$	$f_n = \frac{A\Delta}{T} \sin c^2\left(\frac{nw_0\Delta}{2f}\right)$
2Δ anchura del pulso	
$f(t) = \sum_{n=-\infty}^{\infty} (t-nT)$	$f_n = \frac{1}{T} \quad \forall n$